

Name: _____ Index No. _____

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Candidate's Signature: _____

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Date: _____

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QUANTITATIVE TECHNIQUES

November 2015

Time: 3 hours

**KENYA NATIONAL EXAMINATIONS COUNCIL**

**DIPLOMA IN SUPPLY CHAIN MANAGEMENT
DIPLOMA IN BUSINESS MANAGEMENT
DIPLOMA IN PROJECT MANAGEMENT**

QUANTITATIVE TECHNIQUES**3 hours****INSTRUCTIONS TO CANDIDATES**

Write your name and index number in the spaces provided above.

Sign and write the date of examination in the spaces provided above.

*This paper consists of **SEVEN** questions.*

*Answer any **FIVE** questions in the spaces provided in this question paper.*

All questions carry equal marks.

Present Value table is attached.

Candidates should answer the questions in English.

For Examiner's Use Only

| Question | 1 | 2 | 3 | 4 | 5 | 6 | 7 | TOTAL SCORE |
|--------------------------|----------|----------|----------|----------|----------|----------|----------|--------------------|
| Candidate's Score | | | | | | | | |

This paper consists of 18 printed pages.

Candidates should check the question paper to ascertain that all the pages are printed as indicated and that no questions are missing.

1. (a) Explain **four** assumptions of a linear programming model. (8 marks)

- (b) The information below shows the activities to be carried out during a satellite communication dish installation project.

| Activity | Duration (weeks) |
|----------|------------------|
| 0 - 1 | 4 |
| 0 - 2 | 6 |
| 0 - 3 | 11 |
| 1 - 4 | 3 |
| 1 - 6 | 8 |
| 2 - 4 | 2 |
| 3 - 5 | 7 |
| 4 - 6 | 1 |
| 5 - 6 | 3 |
| 6 - 7 | 10 |
| 7 - 8 | 4 |

- (i) Construct the project network diagram.
(ii) Determine the
(I) critical path.
(II) expected project duration.

(12 marks)

2. (a) Define each of the following terms:

- (i) Paasche's price index.
- (ii) Laspeyres price index.
- (iii) Fischer's ideal price index.
- (iv) index number.

(8 marks)

(b) Explain **three** areas of application for each of the following quantitative techniques in decision making process:

- (i) linear programming.
- (ii) network analysis.
- (iii) inventory control.
- (iv) time series analysis.

(12 marks)

3. (a) The following information relates to a certain raw material used in a local hotel:

| | |
|--|---------------------|
| Annual demand | 3000 units |
| Price per item | Ksh 270 |
| Ordering cost | Ksh 4,200 per order |
| Holding cost is 5% of item price, per year | |
| Lead time | 8 days |
| Working days in a year | 365 |

Determine the:

- (i) Economic Order Quantity (EOQ).
- (ii) re-order point.
- (iii) total cost.

(12 marks)

- (b) The following information shows the number of kilometres covered by cars and the associated cost of maintenance for each car, in a car rental company.

| Car | Kilometres covered | Maintenance costs (Ksh) |
|-----|--------------------|-------------------------|
| A | 80,000 | 96,000 |
| B | 29,000 | 12,000 |
| C | 53,000 | 52,000 |
| D | 13,000 | 16,000 |
| E | 45,000 | 26,000 |

- (i) Compute the regression equation of maintenance costs on kilometres covered.
 (ii) Estimate the maintenance cost for a car that has covered 60,000 kilometres.
 (8 marks)

4. (a) The contents of 3 fruit baskets at Mama Awinja groceries are as follows:

| | |
|---------------|-------------------------------|
| First basket | 1 mango, 2 apples, 3 oranges |
| Second basket | 2 mangoes, 3 apples, 1 orange |
| Third basket | 3 mangoes, 1 apple, 2 oranges |

A fruit basket is picked at random and 2 fruits picked from it randomly, one at a time, without replacement. The two fruits picked were an apple and a mango. Determine the probability that the two fruits picked were from the second basket.

(12 marks)

- (b) The following data shows the production of cement in millions of tonnes in a period of 10 years in ABC Cement Company.

| Year | 1999 | 2000 | 2001 | 2002 | 2003 | 2004 | 2005 | 2006 | 2007 | 2008 |
|--------------------------------|------|------|------|------|------|------|------|------|------|------|
| Production (million tonnes) | 21 | 22 | 23 | 25 | 24 | 23 | 25 | 26 | 28 | 27 |

Using 3 - year moving averages, determine the trend values.

(8 marks)

5. (a) The price of a hair drier, in Kenya shillings, is defined by the function $P = 2650 - 50q$ and the total cost is given by the function $TC = \frac{1}{400}q^2 + 150q + 20,000$; where q is the number of units produced. Determine the
- (i) profit maximising price.
 - (ii) maximum profit.

(10 marks)

- (b) The information below shows the number of chairs and number of computers bought by Mary and Jane from the same shop.

| | Number of chairs | Number of computers |
|------|-------------------------|----------------------------|
| Mary | 1,500 | 4 |
| Jane | 1,340 | 6 |

The total amount paid by Mary and Jane was Ksh 936,500 and Ksh 581,250 respectively. Using the matrix method, determine the unit cost of one

- (i) chair.
- (ii) computer.

(10 marks)

6. (a) A particular company is expected to yield the following cash flows in the next 7 years, as shown in the table below:

| Year | Cash Inflow (Ksh) |
|-------------|--------------------------|
| 2015 | 6,380,000 |
| 2016 | 6,900,000 |
| 2017 | 4,980,000 |
| 2018 | 3,500,000 |
| 2019 | 2,700,000 |
| 2020 | 3,320,000 |
| 2021 | 1,750,000 |

An investor has offered to buy out the company at the start of January 2015, at a total price of Ksh 21,500,000. Using the present value approach, advise the owners of the company on whether to accept the offer. The discount rate is 8%.

(9 marks)

6. (a) A particular company is expected to yield the following cash flows in the next 7 years, as shown in the table below:

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An investor has offered to buy out the company at the start of January 2015, at a total price of Ksh 21,500,000. Using the present value approach, advise the owners of the company on whether to accept the offer. The discount rate is 8%.

(9 marks)

- (b) Two groups of students in colleges, A and B sat for the same examination. College A had 50 students and their mean grade was 75 with a standard deviation of 9. College B had 60 students and their mean grade was 79 with a standard deviation of 7. Test whether there is any significant difference in the performance of the two colleges at 5% level of significance. (11 marks)

7. (a) Distinguish between each of the following terms as used in network analysis:

- (i) succeeding activity and preceding activity.
- (ii) Programme Evaluation Review Technique (PERT) and Critical Path Method (CPM).
- (iii) earliest start time and earliest finish time of an activity.
- (iv) merger events and burst events.

(8 marks)

- (b) A firm has an annual demand of 100,000 units of a certain input material. The order cost per order is Ksh 2,000 and the carrying cost is 10% per annum of the purchase price per unit. The purchase price is Ksh 100 per unit. The firm has to chose between three order size options; 100,000, 50,000 or 25,000 units. Advise the management on the best order size option to adopt in order to minimize their costs. (12 marks)

Table B: Present Value of an Annuity of Sh. 1 Per Period for n Periods:

$$PVIFA_{r,n} = \sum_{t=1}^n \frac{1}{(1+r)^t} = \frac{1 - \frac{1}{(1+r)^n}}{r}$$

| Number of Periods | 1% | 2% | 3% | 4% | 5% | 6% | 7% | 8% | 9% | 10% | 12% | 14% | 15% | 16% | 18% | 20% | 24% | 28% | 32% |
|----------------------|---------|---------|---------|---------|---------|---------|---------|---------|---------|--------|--------|--------|--------|--------|--------|--------|--------|--------|--------|
| 1 | 0.9901 | 0.9804 | 0.9709 | 0.9615 | 0.9524 | 0.9434 | 0.9346 | 0.9259 | 0.9174 | 0.9091 | 0.8929 | 0.8772 | 0.8696 | 0.8621 | 0.8475 | 0.8333 | 0.8065 | 0.7813 | 0.7576 |
| 2 | 1.9704 | 1.9416 | 1.9135 | 1.8861 | 1.8594 | 1.8334 | 1.8080 | 1.7833 | 1.7591 | 1.7355 | 1.6901 | 1.6467 | 1.6257 | 1.6052 | 1.5656 | 1.5278 | 1.4568 | 1.3916 | 1.3315 |
| 3 | 2.9410 | 2.8839 | 2.8286 | 2.7751 | 2.7232 | 2.6730 | 2.6243 | 2.5771 | 2.5313 | 2.4869 | 2.4018 | 2.3216 | 2.2832 | 2.2459 | 2.1743 | 2.1065 | 1.9813 | 1.8684 | 1.7653 |
| 4 | 3.9020 | 3.8077 | 3.7171 | 3.6299 | 3.5450 | 3.4651 | 3.3872 | 3.3121 | 3.2397 | 3.1699 | 3.0373 | 2.9137 | 2.8550 | 2.7982 | 2.6901 | 2.5887 | 2.4043 | 2.2410 | 2.0957 |
| 5 | 4.8534 | 4.7135 | 4.5797 | 4.4518 | 4.3295 | 4.2124 | 4.1002 | 3.9927 | 3.8897 | 3.7908 | 3.6048 | 3.4331 | 3.3527 | 3.2743 | 3.1272 | 2.9906 | 2.7454 | 2.5320 | 2.3452 |
| 6 | 5.7955 | 5.6014 | 5.4172 | 5.2421 | 5.0757 | 4.9173 | 4.7665 | 4.6229 | 4.4859 | 4.3553 | 4.1114 | 3.8887 | 3.7845 | 3.6847 | 3.4976 | 3.3255 | 3.0705 | 2.7994 | 2.5342 |
| 7 | 6.7292 | 6.4720 | 6.2303 | 6.0021 | 5.7864 | 5.5824 | 5.3893 | 5.2064 | 5.0330 | 4.8604 | 4.5638 | 4.2882 | 4.1604 | 4.0386 | 3.8115 | 3.6046 | 3.2423 | 2.9370 | 2.6775 |
| 8 | 7.6517 | 7.3255 | 7.0197 | 6.7327 | 6.4652 | 6.2099 | 5.9713 | 5.7466 | 5.5348 | 5.3349 | 4.9876 | 4.6389 | 4.4873 | 4.3436 | 4.0756 | 3.8372 | 3.4712 | 3.0754 | 2.7602 |
| 9 | 8.5680 | 8.1622 | 7.7861 | 7.4353 | 7.1078 | 6.8017 | 6.5152 | 6.2469 | 5.9952 | 5.7590 | 5.3782 | 4.9464 | 4.7716 | 4.6055 | 4.3030 | 4.0310 | 3.5655 | 3.1442 | 2.8001 |
| 10 | 9.4713 | 8.9826 | 8.5302 | 8.1109 | 7.7217 | 7.3601 | 7.0236 | 6.7101 | 6.4177 | 6.1446 | 5.6602 | 5.2161 | 5.0188 | 4.8337 | 4.4941 | 4.1975 | 3.6819 | 3.2689 | 2.9204 |
| 11 | 10.3676 | 9.7868 | 9.2526 | 8.7625 | 8.3064 | 7.8869 | 7.4947 | 7.1390 | 6.8052 | 6.4951 | 5.9377 | 5.4827 | 5.2337 | 5.0296 | 4.6460 | 4.3071 | 3.7357 | 3.3511 | 2.9776 |
| 12 | 11.2551 | 10.5753 | 9.9540 | 9.3851 | 8.8633 | 8.3838 | 7.9427 | 7.5361 | 7.1607 | 6.8137 | 6.1944 | 5.6803 | 5.4206 | 5.1971 | 4.7932 | 4.4392 | 3.8154 | 3.3689 | 3.0133 |
| 13 | 12.1337 | 11.3484 | 10.6350 | 9.9856 | 9.3936 | 8.8527 | 8.3572 | 7.9038 | 7.4869 | 7.1034 | 6.4231 | 5.8424 | 5.5831 | 5.3423 | 4.9095 | 4.5327 | 3.8124 | 3.4272 | 3.0404 |
| 14 | 13.0037 | 12.1062 | 11.2987 | 10.5631 | 9.8946 | 9.2950 | 8.7455 | 8.2442 | 7.7862 | 7.3667 | 6.6202 | 6.0021 | 5.7245 | 5.4675 | 5.0081 | 4.6106 | 3.9616 | 3.4687 | 3.0595 |
| 15 | 13.8651 | 12.8453 | 11.9379 | 11.1194 | 10.3797 | 9.7122 | 9.1929 | 8.5595 | 8.0607 | 7.6061 | 6.8109 | 6.1422 | 5.8473 | 5.5755 | 5.0916 | 4.6755 | 4.0013 | 3.4834 | 3.0754 |
| 16 | 14.7179 | 13.5777 | 12.5611 | 11.6523 | 10.8328 | 10.1059 | 9.4466 | 8.8514 | 8.3126 | 7.8237 | 6.9740 | 6.2851 | 5.9542 | 5.6885 | 5.1824 | 4.7296 | 4.0333 | 3.5026 | 3.0852 |
| 17 | 15.5623 | 14.2919 | 13.1661 | 12.1657 | 11.2741 | 10.4473 | 9.7632 | 9.1216 | 8.5436 | 8.0216 | 7.1196 | 6.3729 | 6.0472 | 5.7487 | 5.2223 | 4.7746 | 4.0591 | 3.5177 | 3.0971 |
| 18 | 16.3983 | 14.9920 | 13.7655 | 12.6583 | 11.6896 | 10.8325 | 10.0591 | 9.3719 | 8.7556 | 8.2014 | 7.2497 | 6.4674 | 6.1280 | 5.8128 | 5.2722 | 4.8122 | 4.0798 | 3.5294 | 3.1035 |
| 19 | 17.2260 | 15.6785 | 14.3218 | 13.1939 | 12.0853 | 11.181 | 10.3366 | 9.6036 | 8.9501 | 8.3649 | 7.3658 | 6.5504 | 6.1982 | 5.8775 | 5.3162 | 4.8435 | 4.0967 | 3.5386 | 3.1090 |
| 20 | 18.0466 | 16.3514 | 14.8775 | 13.5943 | 12.4672 | 11.4699 | 10.5940 | 9.8181 | 9.1285 | 8.5138 | 7.4894 | 6.6731 | 6.2593 | 5.9288 | 5.3527 | 4.8698 | 4.1103 | 3.5458 | 3.1129 |
| 25 | 22.0232 | 19.5235 | 17.4131 | 15.6271 | 14.0939 | 12.7834 | 11.6536 | 10.6748 | 9.8226 | 9.0770 | 7.8431 | 6.8729 | 6.4641 | 6.0971 | 5.4689 | 4.9476 | 4.1474 | 3.5640 | 3.1220 |
| 30 | 25.8077 | 22.3965 | 19.6004 | 17.2930 | 15.3725 | 13.7648 | 12.4090 | 11.2578 | 10.2737 | 9.4289 | 8.0552 | 7.0027 | 6.5660 | 6.1772 | 5.5168 | 4.9289 | 4.1801 | 3.5693 | 3.1242 |
| 40 | 32.8347 | 27.3555 | 23.1148 | 19.7928 | 17.1591 | 15.0463 | 13.3317 | 11.9246 | 10.7574 | 9.7791 | 8.2438 | 7.1050 | 6.6418 | 6.2395 | 5.5482 | 4.9966 | 4.1859 | 3.5772 | 3.1260 |
| 50 | 39.1961 | 31.4236 | 25.7298 | 21.4822 | 18.2559 | 15.7619 | 13.8907 | 12.2355 | 10.9617 | 9.9148 | 8.3045 | 7.1327 | 6.6605 | 6.2483 | 5.5541 | 4.9995 | 4.1666 | 3.5714 | 3.1280 |
| 60 | 44.8550 | 34.7609 | 27.6266 | 22.6235 | 18.9293 | 16.1614 | 14.0392 | 12.3766 | 11.0480 | 9.9872 | 8.3740 | 7.1401 | 6.6651 | 6.2482 | 5.5553 | 4.9999 | 4.1667 | 3.5714 | 3.1280 |

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